Variability in Sea-Surface Temperature and Sea Ice Patterns from Coupled Data Assimilation, 1850–present

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Motivation

- First, see HadISST vs. NOAA ERSST trends in SST (bottom-right figure)
- Climate feedbacks depend on spatial patterns of SST and sea ice
- Substantial disagreements across existing SST datasets come from different infilling methods applied to unobserved regions
- We don't know how satellite-era trends compare to pre-1980 variability because of the disagreements across datasets
- We need to quantify uncertainty in SST and sea-ice patterns - And identify where additional data could help constrain past variability
- There is an opportunity to combine obs of ship-based SST, land-based air temperature, and sea-level pressure using coupled data assimilation

Methods

Linear Inverse Model (LIM)

- Coupled online data assimilation (DA) with climate models is not feasible, so we build **linear inverse models** (LIMs) to represent climate models
- LIMs contain linear dynamics (L) and stochastic noise (S), which together can reproduce the original statistics of the input climate model





We build "cyclostationary" (monthly) LIMs separately for: - CESM1, CESM2, MRI-ESM2-0, HadCM3, GISS-E2R

$$\mathbf{L}_{j} = \tau^{-1} \ln[\mathbf{C}_{j}(\tau)\mathbf{C}_{j}(0)^{-1}], \ j = 1, ..., 12 \ (months); \ \tau = 1$$

(Shin et al. 2021; Penland & Sardeshmukh 1995)

Data Assimilation (DA)

- LIM produces monthly "prior" forecasts, and the Kalman filter produces the "posterior" analysis (accounting for model and observation uncertainty)
- Forecasts are launched from previous analysis (i.e., this DA framework has "memory" of past observations)

Ensemble Mean (x) $\mathbf{G}_i = \exp(\mathbf{L}_i \delta t)$ 1) Forecast: $\mathbf{x}_{\mathbf{f}}(t + \delta t) = \mathbf{G}_{i}\mathbf{x}_{\mathbf{a}}(t) + \mathbf{n}$ 2) Assimilation: $\mathbf{x}_{a} = \mathbf{x}_{f} + \mathbf{K}(\mathbf{y} - \mathbf{H}\mathbf{x}_{f})$ $\mathbf{K} = \mathbf{P}_{\mathbf{f}} \mathbf{H}^{\mathrm{T}} [\mathbf{H} \mathbf{P}_{\mathbf{f}} \mathbf{H}^{\mathrm{T}} + \mathbf{R}]^{-1}$ **Covariance** (P)

1)	Forecast:	$\mathbf{P}_{\mathbf{f}}(t+\delta t) = \mathbf{G}_{j}\mathbf{P}_{\mathbf{a}}\mathbf{G}_{j}^{\mathrm{T}} + \mathbf{N}_{j}$
		$\mathbf{N}_j = \boldsymbol{C}_j(0) - \mathbf{G}_j \boldsymbol{C}_j(0) \mathbf{G}_j^{\mathrm{T}}$
2)	Assimilation	: $P_a = (I - KH)P_f$



Conclusions & Next Steps

- We combine models and observations to produce spatially complete monthly SST, 2-m air temp., and sea-level pressure back to 1850
- LIM+DA method captures large-scale variability and trends, but perhaps more importantly, quantifies uncertainty and its spatial fingerprints
- Results could be used in atmospheric GCMs to investigate uncertainty in **historical feedbacks** and its sources in the Tropics, Southern Ocean, etc.
- Method could be extended to investigate past variability in the hydrologic cycle (P–E)

Std. Deviation of Nino3.4 by Month

10 11 12

Illustration of LIM + DA Method — Truth (GCM) Posterior Mear

(Hakim et al. 2022)

- and sea-level pressure are assimilated
- draw obs from a target climate model (GFDL-CM4 shown below)

to replicate the actual obs









- Reconstruction of sea ice is a work-in**progress**: challenges come from different mean states and physics in models vs. reality
- Uncertainties in sea ice (and implications) for feedbacks) need to be quantified given differences in existing gridded datasets (see figure at right)